

Progresii

1. Fie progresia aritmetica $a_1, a_2, \dots, a_n, \dots$, $n \in \mathbf{N}$

$$\begin{aligned}d &= a_n - a_{n-1}; & a_n &= a_1 + d(n-1); \\S_n &= \frac{a_1 + a_n}{2}n; & S_n &= \frac{2a_1 + d(n-1)}{2}\end{aligned}$$

unde d - ratia progresiei, a_n - termenul de rang n , S_n - suma primilor n termeni ai progresiei.

2. Fie progresia geometrica $b_1, b_2, \dots, b_n, \dots$, $n \in \mathbf{N}$

$$\begin{aligned}q &= \frac{b_n}{b_{n-1}}; \\b_n &= b_1q^{n-1}; \\S_n &= \frac{a_nq - a_1}{q - 1} \quad \left(S_n = \frac{a_1 - a_nq}{1 - q} \right); \\S_n &= \frac{a_1(q^n - 1)}{q - 1} \quad \left(S_n = \frac{a_1(1 - q)^n}{1 - q} \right)\end{aligned}$$

unde q - ratia progresiei, S_n - suma primilor n termeni ai progresiei.

Suma progresiei geometrice infinit descrescatoare este

$$S = \frac{b_1}{1 - q}$$

unde $|q| < 1$.