# Deductive databases and P systems

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#### Abstract

In computational processes based on backwards chaining, a rule of the type  $A \leftarrow B_1, \ldots, B_n$  is seen as a procedure which points that the problem A can be split into the problems  $B_1, \ldots, B_n$ . In classical devices, the subproblems  $B_1, \ldots, B_n$  are solved sequentially. In this paper we present some questions that circulated during the Second Brainstorming Week related to the application of the parallelism of P systems to computation based on backwards chaining on the example of inferential deductive process.

**Keywords:** artificial intelligence, Deductive databases, P systems, membrane systems, backwards chaining, inferential deductive process

#### 1 Introduction

In computational processes based on backwards chaining, a rule of the type  $A \leftarrow B_1, \ldots, B_n$  is usually seen as a procedure which points that the problem A can be split into the problems  $B_1, \ldots, B_n$  with the hope that  $B_1, \ldots, B_n$  are simpler than A. In the case of getting  $B_1, \ldots, B_n$  solved, we also have a solution for A via this rule.

This is the case of pure Prolog [2, 10] where  $A \leftarrow B_1, \ldots, B_n$  is a definite clause and  $A, B_1, \ldots, B_n$  are positive literals. Prolog uses SLD resolution to find an answer to the goal A, i.e., Linear resolution for Definite clauses with Selection function. This selection function considers sequentially the list of current subgoals  $B_1, \ldots, B_n$  and chooses one of them (in standard Prolog the selection function always takes the leftmost literal). The process of finding an answer for the chosen

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subgoals generates new subgoals, hopefully simpler than the previous one. The computation ends when trivial subgoals are reached.

The selection mapping is necessary because classic computational devices work sequentially, so we need to fix an order between the tasks.

In this paper we present some questions that circulated during the Second Brainstorming Week related to the application of the parallelism of P systems to the computation based on backwards chaining.

### 2 Logic Programming

Although the computation based on backwards chaining is a general procedure in Computer Science, we focus our attention on Deductive Databases and Logic Programming.

The way of representing information in Logic Programming (e.g. [1, 3, 6, 8, 4]) is via a set of clauses. These sets of clauses are *logic* programs. Roughly speaking, a clause is a first-order rule, where both sides of the rule consist of atoms, i.e, a predicate applied to some arguments. Formally, a clause is a formula

$$\forall x_1 \dots \forall x_s A_1 \vee \dots A_k \vee \neg B_1 \vee \dots \vee \neg B_n$$

where  $x_1, \ldots, x_s$  are all the variables that occur in the atoms  $A_1, \ldots, A_k$ ,  $B_1, \ldots, B_n$ . A clause<sup>1</sup> is a *Horn clause* if it contains at most one positive literal (atom) and it is a *definite clause* if it contains exactly one positive literal. For example

$$\forall X \forall Y \ daughter(X,Y) \lor \neg female(X) \lor \neg mother(Y,X)$$

is a definite clause. This universally quantified formula is usually written as

$$daughter(X,Y) \leftarrow female(X), mother(Y,X)$$

The positive literal, i.e. the *conclusion* of the implication is usually called the *head* of the clause. The rest of the literals, the *premises*, are

 $<sup>^{1}</sup>$ The basic difference between program clauses and database clauses is the use of types.

known as the *body* or the *tail* of the clause. Definite clauses can consist of a single positive literal. They can be considered as rules with no tail or no conditional sentences, as

$$female(anne) \leftarrow \\ mother(mary, anne) \leftarrow$$

These clauses are facts. A substitution  $\theta = \{V_1/t_1, \dots, V_n/t_n\}$  is an assignment of terms  $t_i$  to variables  $V_i$ . If a substitution is applied to a clause we get an instantiated clause, where all occurrences of the variable  $V_i$  are replaced by the term  $t_i$ . For example, if the substitution  $\theta = \{X/anne\}$  is applied to the clause C:

$$daughter(X, Y) \leftarrow female(X), mother(Y, X)$$

we get the clause  $C\theta$ :

$$daughter(anne, Y) \leftarrow female(anne), mother(Y, anne)$$

A substitution  $\theta$  is a unifier of the atoms A and B if  $A\theta = B\theta$ .

Logic programs compute through a combination of two mechanisms: unification and resolution. From any two clauses with complementary literals A and  $\neg A$  the inference rule of resolution derives a new clause as consequence. For example, from

$$\begin{aligned} daughter(anne, Y) \leftarrow female(anne), mother(Y, anne) \\ female(anne) \leftarrow \end{aligned}$$

we obtain the clause  $daughter(anne, Y) \leftarrow mother(Y, anne)$ . The deduction process is a goal driven in the following way. If we have the program

$$daughter(X, Y) \leftarrow female(X), mother(Y, X)$$
  
 $female(anne) \leftarrow$   
 $mother(mary, anne) \leftarrow$ 

and we want to know if daughter(anne, mary) is true, first we build the goal

$$\leftarrow daughter(anne, mary)$$

i.e., the one-literal clause  $\neg daughter(anne, mary)$ . The atoms daughter(anne, mary) and daughter(X, Y) unify with the substitution  $\theta = \{X/anne, Y/mary\}$ . By using resolution with the first clause of the program and the unifier  $\theta$  we get the new goal

 $\leftarrow female(anne), mother(mary, anne)$ 

As we saw before, this step can be seen in a procedural mode. The problem of deciding if daughter(anne, mary) is true has been split into two subproblems: Decide if female(anne) and mother(mary, anne) are true or not. But they are true because they are claimed by our program, so daughter(anne, mary) is true.

When the reasoning system solves the  $goal\ Q$  it gives us an answer. There are two types of outputs given by the system with respect to the type of the goal Q:

- 1. If the goal does not contain variables, we have a decision problem, and the possible answers are Yes or No. In this case the system decides if the goal can be or not derived form the program.
- 2. If the goal contains variables, the system outputs the unifier  $\theta$  such that the instantiated goal  $Q\theta$  can be derived from the problem. This unifier represents the answer to the question, and obviously several unifications  $\theta$  that make the goal  $Q\theta$  true can exist.

In our example, we deal with a decision problem. After the first step the subgoals female(anne) and mother(mary, anne) have to be solved. This is done sequentially in classical devices with only one processor. We wonder if it is possible to use P systems for these problems. We think that it would be very interesting to use the parallelism of P systems to solve all subgoals in parallel manner.

## 3 P systems

Now we are going to show some hints about a general representation of a set of typed definite clauses (Deductive Database) and of the inferential

deductive process in the frame of hierarchical P systems [9] with active membranes [5].

Let us consider Deductive Database (DDB)

$$Q_{1} \leftarrow P_{11}, P_{12}, \dots, P_{1m}$$

$$Q_{2} \leftarrow P_{21}, P_{22}, \dots, P_{2m}$$

$$\dots \dots \dots \dots$$

$$Q_{n} \leftarrow P_{n1}, P_{n2}, \dots, P_{nm}$$

We assume for simplicity that we have the same set of parameters  $\{x_1, \ldots, x_s\} \in D^s$  from the same domain D for all literals  $Q_i$ ,  $i \in \{1, \ldots, n\}$ ,  $P_{ij}$ ,  $i \in \{1, \ldots, n\}$ ,  $j \in \{1, \ldots, m\}$ , and the same order of parameters  $(x_1, \ldots, x_s)$  for heads of all rules. Literals from tails are allowed to have any order of parameters.

We can ask goals presented as literals with constant terms and/or variables in the set of parameters to the inferential deductive machine. Constants will be denoted by  $c_i$  and variables will be denoted by  $v_i$ . We assume that goal have the same order of parameters  $(x_1, \ldots, x_s)$  as heads of DDB clauses.

Now we will give the general model of logic inferential deductive machine and some ideas how it can be represented in the frame of P systems. Consider the DDB described above and the goal Q. Logic inferential deduction process will be performed recursively conform the following steps:

# ALGORITHM: SOLVE INPUT: Q

#### PART 1: From the goal to the axioms:

**Step 1** Head unification: Unification of Q with all heads  $Q_i$  from DDB in parallel. As the result every head  $Q_i$  for which the unification process succeeded will get the set of unifiers  $\theta_i$ .

**Step 2** Body unification: For every head  $Q_i$  for which step 1 succeeded and the tail is not empty, body unification process will be performed with all subgoals  $P_{ij}$  in parallel, that is the algorithm SOLVE

will be launched in parallel for every subgoal  $P_{ij}$  with input  $P_{ij}\theta_i$ . In the case of facts (rules with empty tail) the system returns the unifier  $\theta_i$  of the head  $Q_i$ .

#### PART 2: From the axioms to the goal

**Step 3** Atom unification: For every rule for which step 2 succeeded, the unification of results of all subgoals is performed.

**Step 4** Union of the results: Since every particular rule from the DDB gives us some set of unifiers (solutions), one should consider the union of all these sets as a solution of Q.

**OUTPUT:** There are possible two cases:

- 1. The result to be the set of all unifiers  $\Theta = \{\theta | DDB \vdash Q\theta\}$ . In other words, the result will be the set of all unifiers  $\theta$  for which  $Q\theta$  could be derived from DDB
- 2. The result to be Yes in the case  $\Theta = \{\theta\}, Q = Q\theta$  and No in the case  $\Theta = \emptyset$

In this way we have got two types of parallelism here:

- 1. For each head  $Q_i$  a process which unifies it with Q and which unifies results of subgoals  $P_{ij}$  is created;
- 2. For each subgoal  $P_{ij}$  of  $Q_i$  the solving process is created.

In Fig.1 the general scheme of the deduction process and of the parallel processes interactions is presented. For each process from the scheme a membrane is created. In this way one can treat the tree of the processes interaction as a hierarchy of membranes of the P system solving the problem.

One can define two general types of membranes:

1. Membranes which stay for goals and subgoals representation. Membranes of this type perform steps 1 and 4. On the Step 1 they create submembranes which stay for the heads of the clauses. On the Step 4 it collects results of the inferential rules execution.

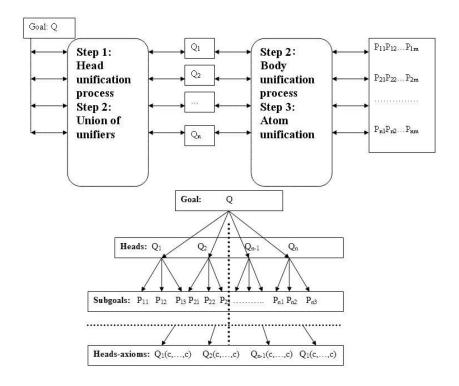


Figure 1. The general scheme of the deduction process and of the processes interaction

- 2. Membranes which stay for clause's heads representation. They perform  $steps\ 2$  and 3. For this type of membranes there are possible two cases:
  - The tail is not empty: membranes complete term unification of the head and goal, create submembranes which stay for the subgoals, perform term unification with all subgoals.

The tail is empty: membranes complete term unification.

All these ideas need to be concretized and formalized, of course, what will be possible in future research of the problem.

#### 4 Final remarks

In this work-in-progress paper we describe some preliminary ideas born from discussions about this topic during the Second Brainstorming Week. This is only the beginning and a lot of work have to be done. The first step is to fix the backwards chaining formalism that we want to study in P systems. Function-free clauses, i.e., clauses which contain only variables as terms can be a good starting point, but to handle relevant information Datalog [11] clauses can be more suitable. Datalog clauses are definite clauses that contain no functions symbols of non-zero arity. As we have seen, we have a long path to walk.

The preliminary version of this paper one can find in [12].

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